

Dérivée des fonctions usuelles.

★ Si $f(x) = cste$ (fonction constante)

donc $f'(x) = 0$; $\forall x \in \mathbb{R}$

Exemples: $f(x) = 5$; $f(x) = \frac{15}{2}$
donc $f'(x) = 0$; donc $f'(x) = 0$

★ Si $f(x) = ax + b$; $x \in \mathbb{R}$

donc $f'(x) = a$

Exemples $f(x) = 2x - 1$; $f(x) = \frac{2}{3}x - \frac{5}{2}$
donc $f'(x) = 2$; $f'(x) = \frac{2}{3}$

★ Si $f(x) = x^n$; $n \geq 2$

donc $f'(x) = nx^{n-1}$; $\forall x \in \mathbb{R}$

Exemples: $f(x) = x^4$; $f(x) = x^{17}$
donc $f'(x) = 4x^3$; $f'(x) = 17x^{16}$

★ Si $f(x) = \frac{1}{x}$; $\forall x \in \mathbb{R}'$





donc $f'(x) = -\frac{1}{x^2}$

exemples:

$f(x) = \frac{4}{x}$ donc $f'(x) = -\frac{4}{x^2}$

$f(x) = -\frac{3}{x}$ donc $f'(x) = \frac{3}{x}$

♦ Si $f(x) = \sqrt{x}$; $\forall x \in \mathbb{R}_+$
donc $f'(x) = \frac{1}{2\sqrt{x}}$

♦ Si $f(x) = \sin(ax+b)$; $\forall x \in \mathbb{R}$
donc $f'(x) = a \cos(ax+b)$

exemple:

$f(x) = \sin(2x-4)$; $\forall x \in \mathbb{R}$
donc $f'(x) = 2 \cos(2x-4)$

♦ Si $f(x) = \cos(ax+b)$; $\forall x \in \mathbb{R}$
donc $f'(x) = -a \sin(ax+b)$



Example:

$$f(x) = \cos\left(4x + \frac{1}{3}\right) ; \forall x \in \mathbb{R}$$

$$\text{donc } f'(x) = -4 \sin\left(4x + \frac{1}{3}\right)$$

$$\star \text{ Si } f(x) = \operatorname{tg}(x) ; x \in \mathbb{R} \setminus \left\{ \frac{\pi}{2} + k\pi, k \in \mathbb{Z} \right\}$$

$$\text{donc } f'(x) = 1 + \operatorname{tg}^2 x \\ = \frac{1}{\cos^2 x}$$

$$\star \text{ Si } f(x) = \operatorname{cotg}(x) ; x \in \mathbb{R} \setminus \{ k\pi, k \in \mathbb{Z} \}$$

$$\text{donc } f'(x) = 1 + \operatorname{cotg}^2 x \\ = \frac{1}{\sin^2 x}$$